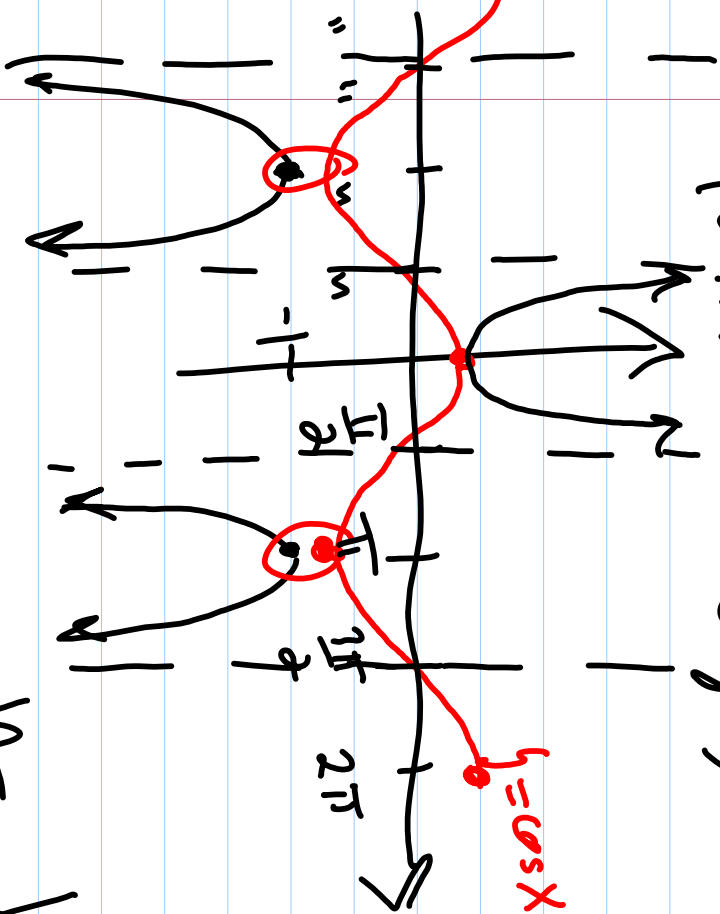
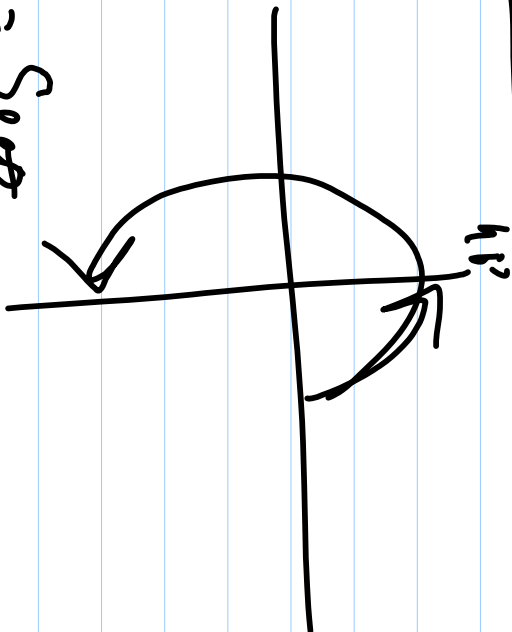


Exam Review

Part A (Knowledge)



Vals at $X = \frac{\pi}{2}, \frac{3\pi}{2}$



$$y = \cos \theta = \sin \theta \quad 270^\circ$$

B

$$2) \quad y = 40 \cos \left[\frac{2\pi}{12} x \right]$$

$$y = 40 \sin \frac{2\pi}{12} x$$

$$\frac{2\pi}{12} = \frac{\pi}{6}$$

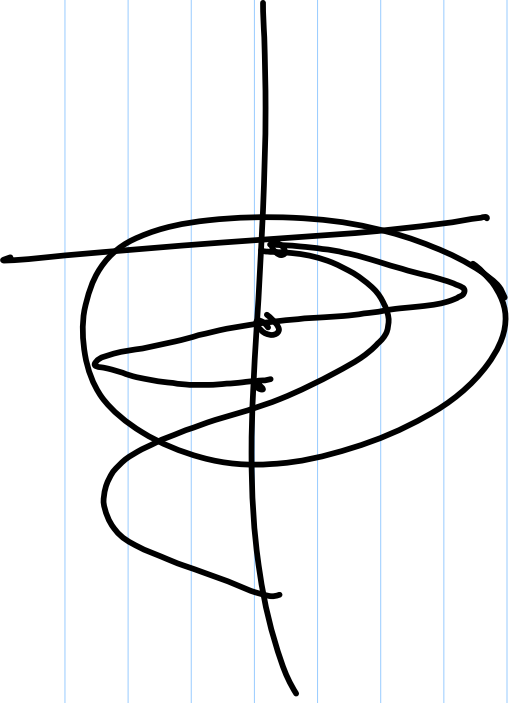
$$12 = \frac{2\pi}{\frac{\pi}{6}}$$

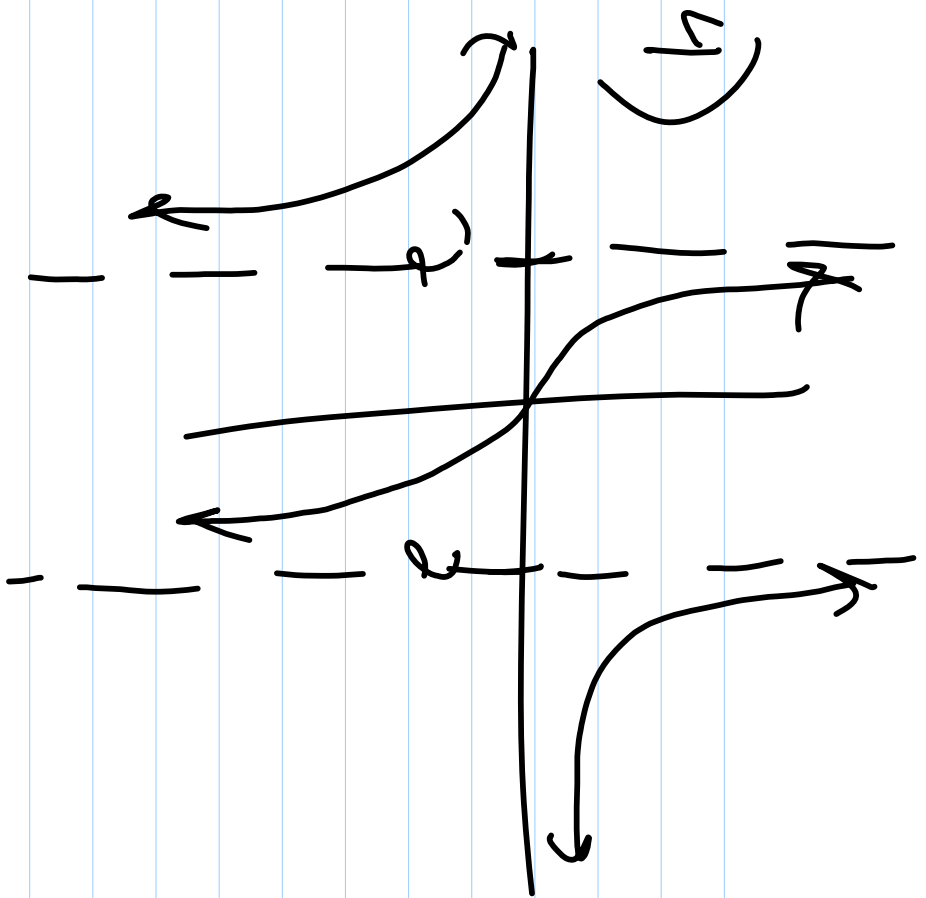
$$= 12$$

$$y = 5 \sin 4x$$

$$k = 4$$

$$p = \frac{2\pi}{k} = \frac{2\pi}{4}$$



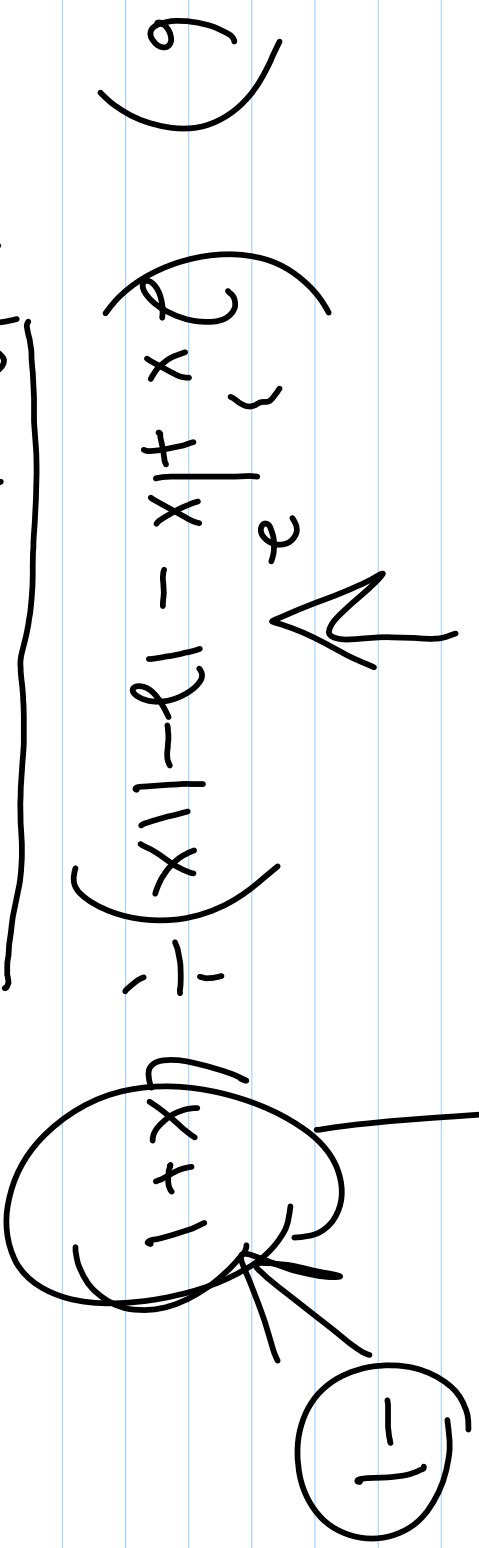


A. ~~$y = \frac{-x^2}{x^2 - 4}$~~

B. $y = \frac{x}{x^2 - 4}$

C. ~~$y = \frac{x^2}{x^2 - 4}$~~

D. ~~$y = \frac{x^2 - 4}{x^2}$~~



$$\frac{-1 | 2 | - 1 | - 1 |}{-}$$

$$\begin{array}{r} + \quad | \quad -2 \quad | \quad 1 \quad | \quad 10 \\ \hline \cancel{2} \quad \cancel{1} \quad \cancel{-10} \quad | \quad \boxed{-2R} \end{array}$$

$$p(x) = d(x)q(x) + R,$$

$$p(x) = (x+1)(2x^2 - x - 10) + (-2)$$

$$\begin{array}{l} \rightarrow \\ \rightarrow \end{array} \quad (x^4 - 4x^2 + 5x - 1) \div (x-2) = 2$$

$$p(2) = \# \quad R \quad \text{by R.T.}$$

$$2^4 - 4(2)^2 + 5(2) - 1 = 9 \text{ R.}$$

8) Solve.

Factor!!!

a) $x^3 - 4x^2 - 7x + 10 = 0$

Factors: $(x-2)(x+1)(x) = 0$

b) $\frac{7x+3}{x^2+x} = \frac{2}{x+1}$

$$7x+3 = 2x^2+2x$$

$$0 = 2x^2 - 5x - 3$$

$$0 = 2x^2 - 6x + x - 3$$

$$0 = 2x(x-3) + 1(x-3)$$

$P(1) = 0$ R by R.T.
 $(x-1)$ factor by F.T.

$$\begin{array}{cccc|cccc} 1 & 1 & -4 & -7 & 1 & 0 & & \\ \hline & & & & & & & \end{array}$$

$$0 = (2x+1)(x-3)$$

Ans: $x = -\frac{1}{2}, +3$

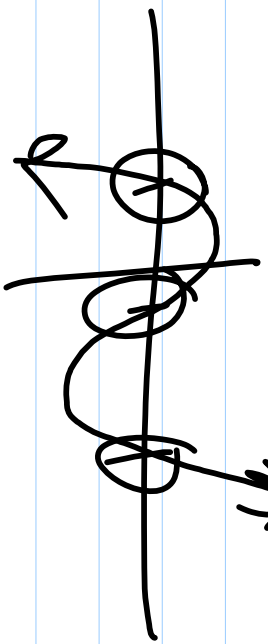
$$\begin{array}{cccc|cccc} 4 & 1 & -3 & -16 & & & & \\ \hline & & & & & & & \end{array}$$

$\left[\begin{array}{cc} -3 & -16 \end{array} \right]$ OR

$$P(x) = (x-1)(x^2-3x-16) \text{ w.r.}$$

more factors.

$$= (x-1)(x-5)(x+2) \text{ Ans: } x = 1, -2, 5$$



$$\textcircled{1} \quad \frac{x^2 + 2x - 9}{(x-1)(x-3)} < 0$$

$$(x-1)(x-3)$$

$$\frac{(x-3)(x+2) - (x+1)(x-1)}{(x-1)(x-3)} < 0$$

$$\frac{x^2 + 2x - 9}{(x-1)(x-3)} < 0$$

Partial fraction decomposition:

$$\frac{x^2 + 2x - 9}{(x-1)(x-3)} = \frac{A}{x-1} + \frac{B}{x-3}$$
$$\frac{x^2 + 2x - 9}{(x-1)(x-3)} = \frac{A(x-3) + B(x-1)}{(x-1)(x-3)}$$
$$x^2 + 2x - 9 = A(x-3) + B(x-1)$$
$$x^2 + 2x - 9 = Ax - 3A + Bx - B$$
$$x^2 + 2x - 9 = (A+B)x - (3A+B)$$
$$\begin{cases} A+B = 2 \\ -3A-B = -9 \end{cases}$$
$$\begin{matrix} + & - & + \\ \hline 2 & - & -9 \end{matrix}$$
$$\begin{matrix} + & - & + \\ \hline 2 & - & -9 \end{matrix}$$

Sign chart for $\frac{x^2 + 2x - 9}{(x-1)(x-3)} < 0$:

$x < -3$	$-3 < x < -1$	$-1 < x < 3$	$x > 3$
+	-	+	-

Roots: $x = -3$ and $x = 3$ are circled. Arrows indicate the direction of the inequality.

$$\frac{\cancel{\phi(x)}}{\cancel{\phi(x)}} \rightarrow +\infty$$

$$\frac{(x-5)^{-2}}{(x-1)(x-3)}$$

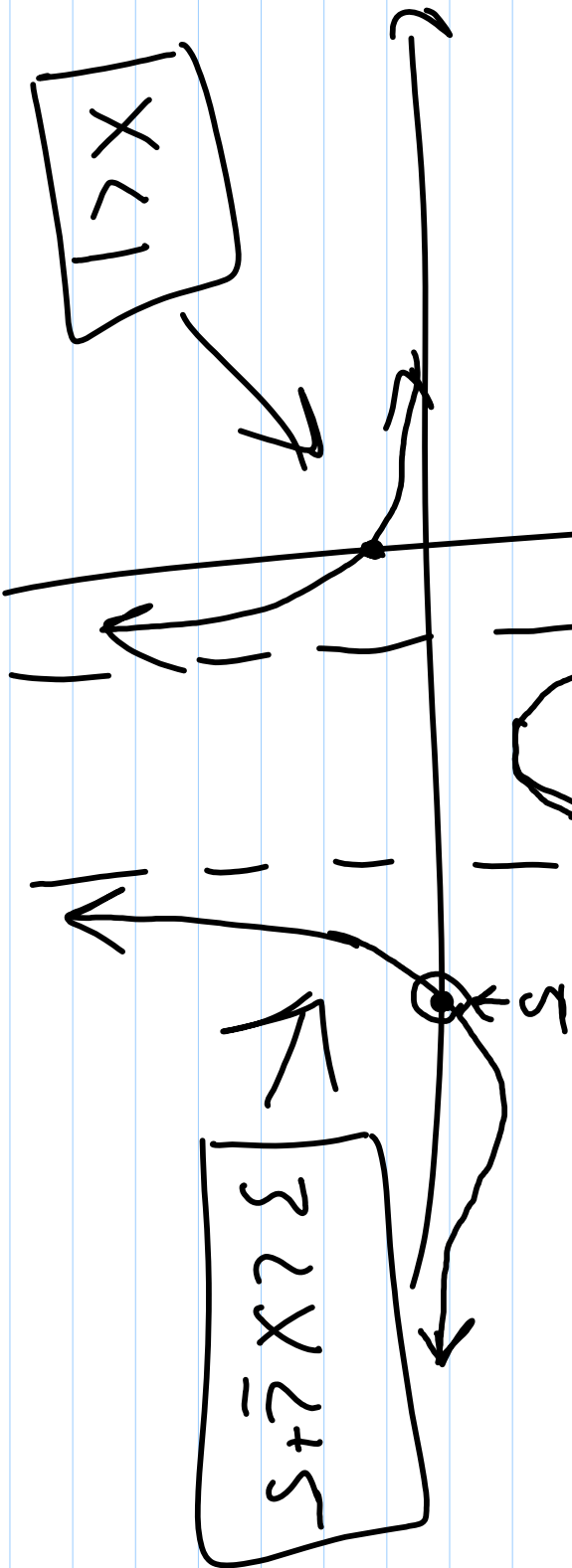
$$\frac{-\#}{\#(x-1)}$$

$$\frac{1}{(x-1)}$$

$$\frac{(x-1)(x-3)}{(x-1)(x-3)}$$

$$\frac{-\#}{\#(x-1)} \rightarrow -\infty$$

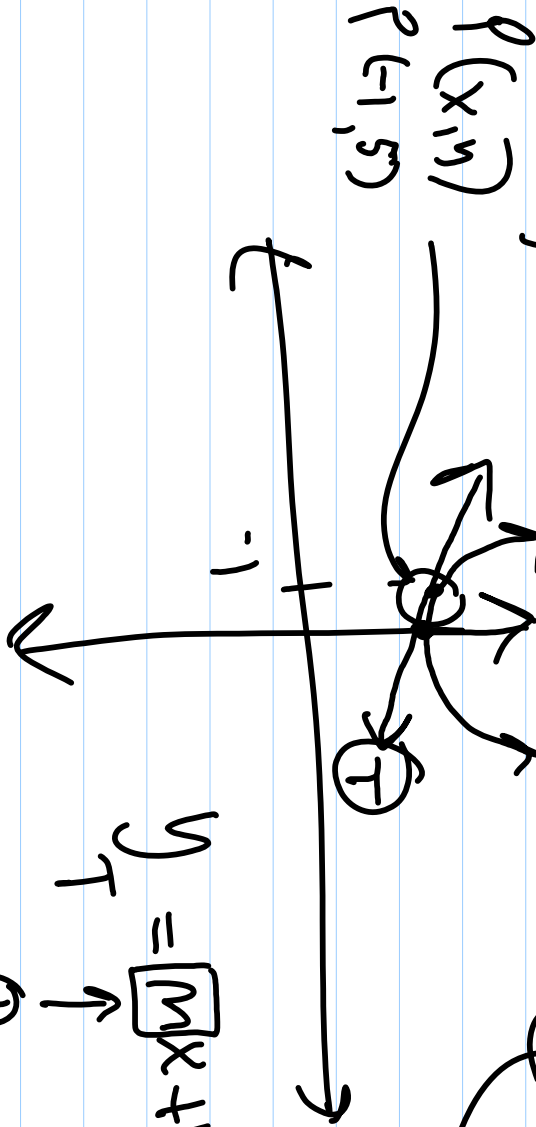
~~AA~~
 $y=0$



10) Tangent Eqn:

$$f(x) = x^2 - x + 3$$

$$x = -1$$



$$y_T = \boxed{m}x + \boxed{b}$$

① → ② →

$$f'(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x+\Delta x) - f(x)}{\Delta x}$$

$f'(-1)$

$$f'(-1) = \lim_{\Delta x \rightarrow 0} \frac{f(-1+\Delta x) - f(-1)}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{[(-1+\Delta x)^2 - (-1+\Delta x) + 3] - 5}{\Delta x}$$

\downarrow

\downarrow

5

$$(1+x)(1+x^2)(1+x^4) \dots (1+x^{2^{n-1}})$$

$$= \lim_{\Delta x \rightarrow 0} \frac{1 - \cancel{2\Delta x} + \cancel{\Delta x} + 1 - \cancel{\Delta x} + 3 - 5 - \dots}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{\Delta x^2 - 3\Delta x}{\Delta x}$$

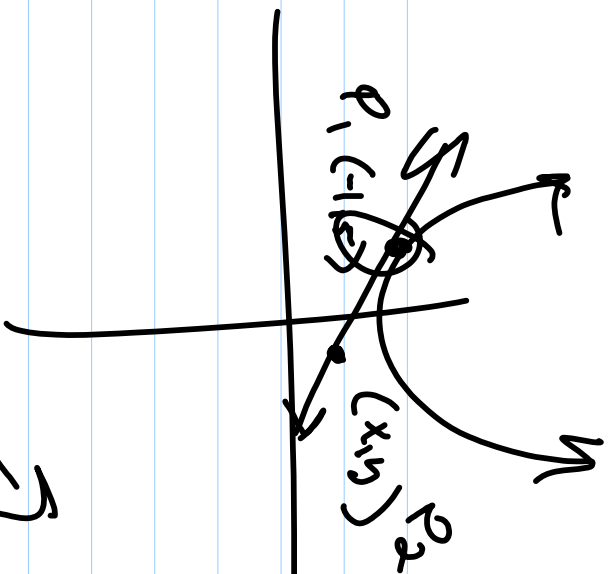
$$= \lim_{\Delta x \rightarrow 0} \frac{\cancel{\Delta x}(\Delta x - 3)}{\cancel{\Delta x}}$$

$$= \lim_{\Delta x \rightarrow 0} (\Delta x - 3)$$

$$= -3$$

$$M_T = -3$$

$$y_T = M_T'X + b$$



$$y_2 - y_1 = m(x_2 - x_1)$$

$$(y_2 - y_1) = m(x_2 - x_1)$$

$$y - 5 = -3(x - (-1))$$

$$y - 5 = -3(x + 1)$$

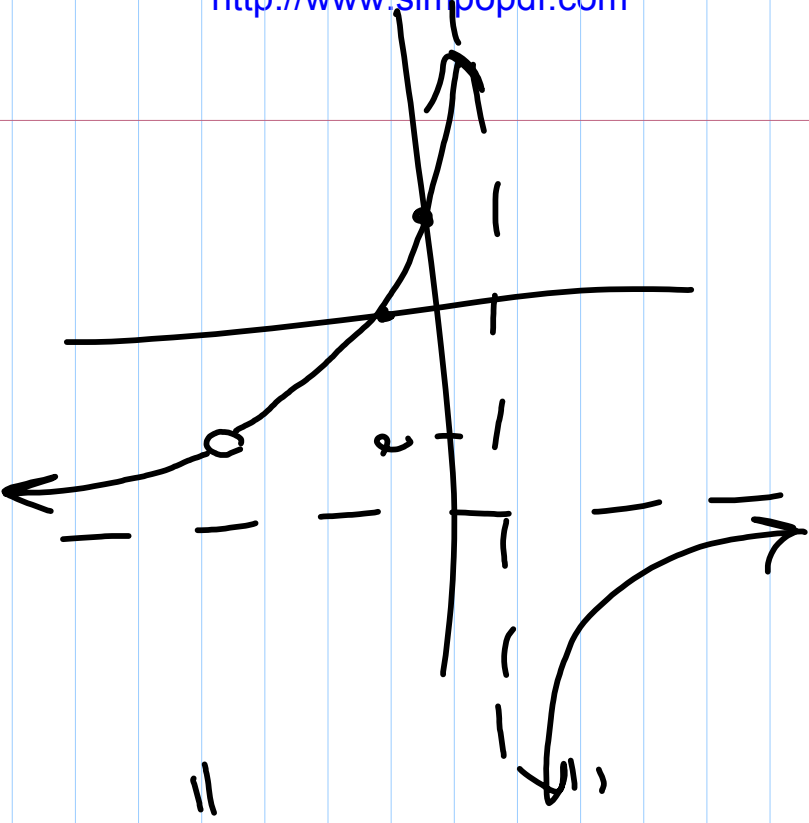
$$y = -3x - 3 + 5$$
$$y = -3x + 2$$

10) $f(x) = \frac{x^2 - x - 2}{e - x - 2}$

~~$(x-2)(x+1)$~~ $(x-2)$ $(x+1)$ $(x-2)$

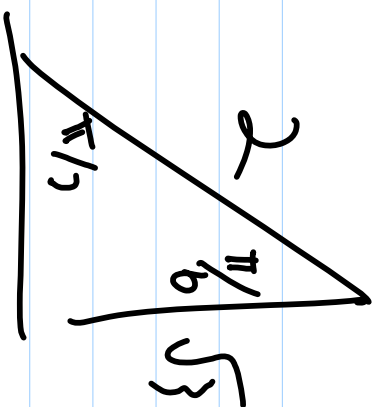
Nullstelle
 $x = 2$

$s = 1$ ~~11~~ $\frac{x+1}{x-3}$



Part B: Apes.

1) Solve for x $0 \leq x < 2\pi$.



Refer to my p+2 test (Skill 5),

$$a) \quad y = \cos x + q \quad \left(\frac{\pi}{3}, 1 \right)$$

$$1 = \cos \frac{\pi}{3} + q$$

$\rightarrow q = 1 - \frac{1}{2} = \frac{1}{2}$

$$q = 1 - \cos\left(\frac{\pi}{3}\right)$$

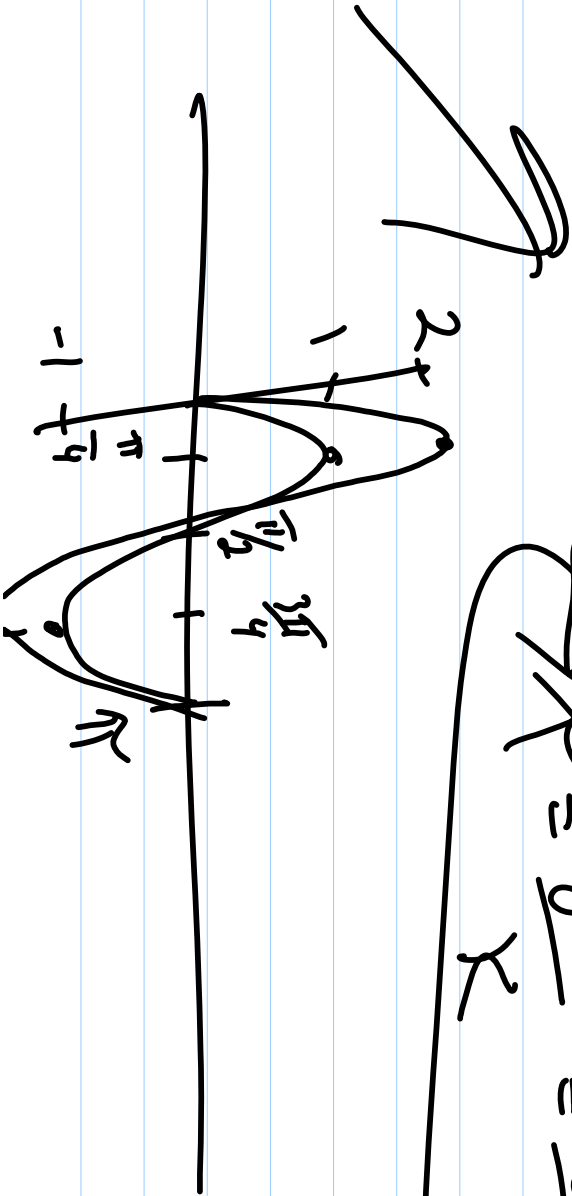
$\rightarrow y = \cos x + \frac{1}{2}$

3)

$$y = 2 \sin \left(2x + \frac{\pi}{4} \right) - 1$$

$$= \sqrt{2} \left[\sin \left(2x + \frac{\pi}{4} \right) \right] - 1$$

$$\frac{\pi}{4} = \frac{2\pi}{4} = \frac{\pi}{2} = \frac{\pi}{2}$$



$$4) y = 2 \sin\left(\frac{1}{2}x + \frac{\pi}{2}\right) + 1$$

$$= 2 \sin \frac{1}{2} (x + \pi) + 1$$

a.) $\rho_s \leftarrow \sqrt{1}$ mit b) $\rho = \frac{2\pi}{k} = \frac{2\pi}{\frac{1}{2}} = 4\pi$

c) z d) z_{\max} e) -1 f) $-1 \leq y \leq 3$

g) $| \uparrow$

5) Solve

a) $(2\cos x + \sqrt{3})(\cos x - 1) = 0$

$2\pi < x < 2\pi$

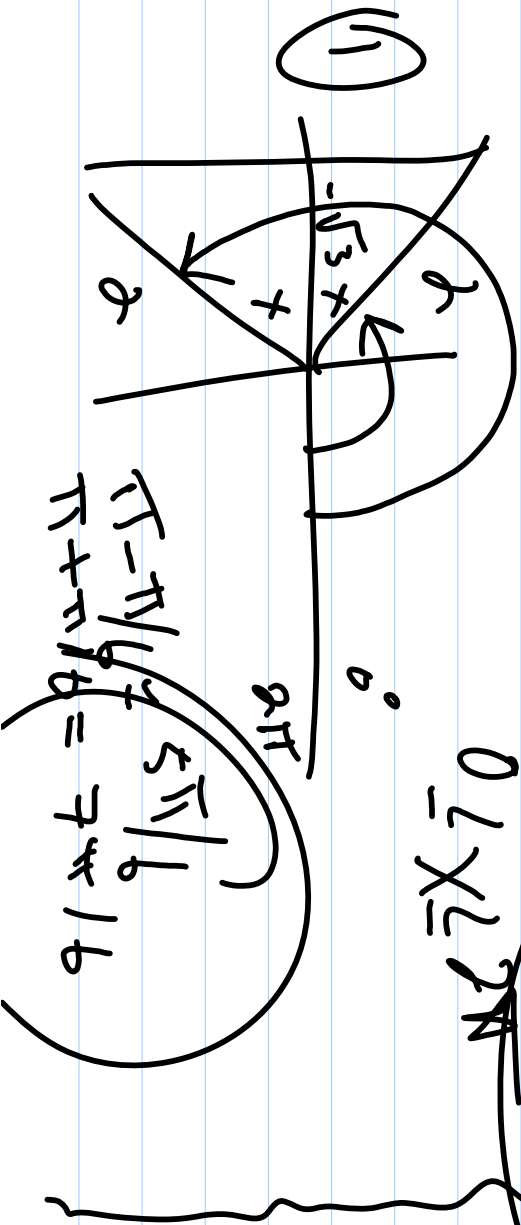
$\Rightarrow \textcircled{1} \quad 2\cos x + \sqrt{3} = 0 \Rightarrow \cos x = -\frac{\sqrt{3}}{2}$

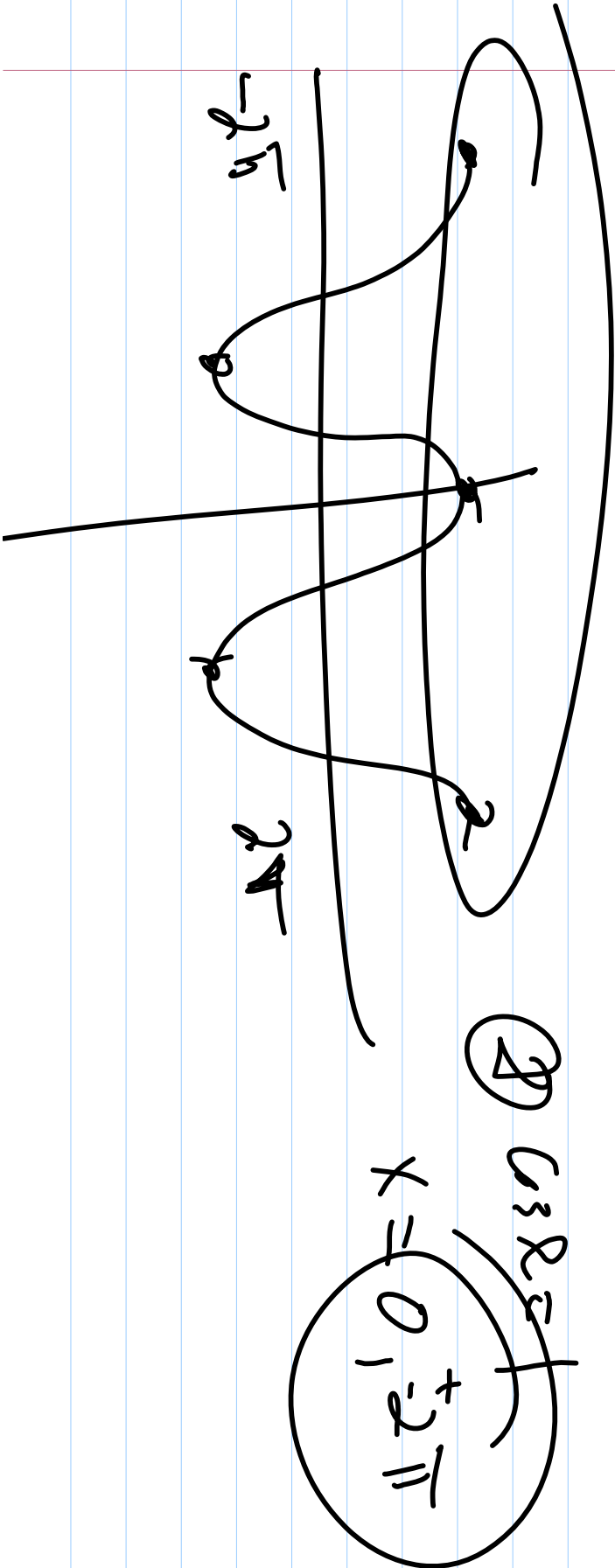
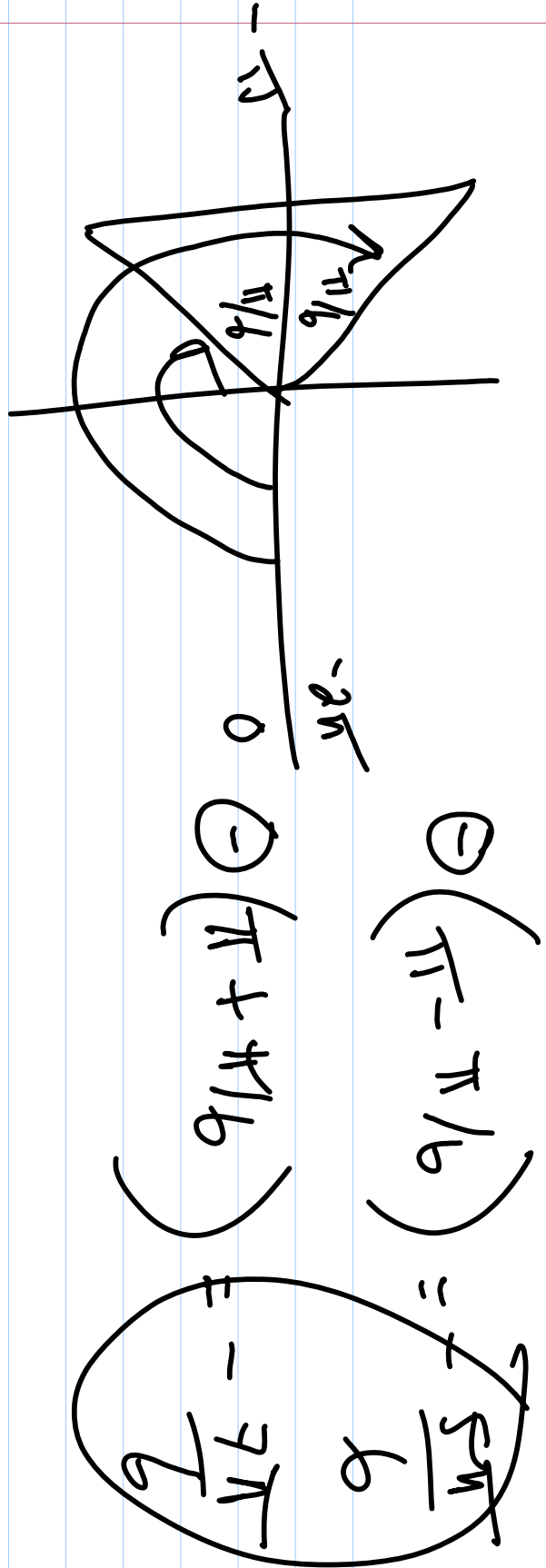
$\textcircled{2} \quad \cos x - 1 = 0$

$\Rightarrow \cos x = 1$

$0 < x < 2\pi$

$2\pi < x < 0$





$$b) 3(2)^x = 12^{x-1}$$

$$\log(3)(2)^x = \log 12^{x-1}$$

$$\log 3 + \log 2^x = (x-1) \log 12$$

$$\log 3 + x \log 2 = x(\log 12) - \log 12$$

$$x \log 2 - x \log 12 = -\log 3 - \log 12$$

$$x(\log 2 - \log 12) = \underline{-\log 3 - \log 12}$$

$$\boxed{X = 2}$$



$$\log 3^{-1} = \log 12$$

$$\log \frac{1}{3} = \log 12$$

$$\log \frac{113}{12}$$

$$\boxed{\log \frac{1}{36}}$$

$$\log \frac{2}{12}$$

$$\log \frac{1}{6}$$

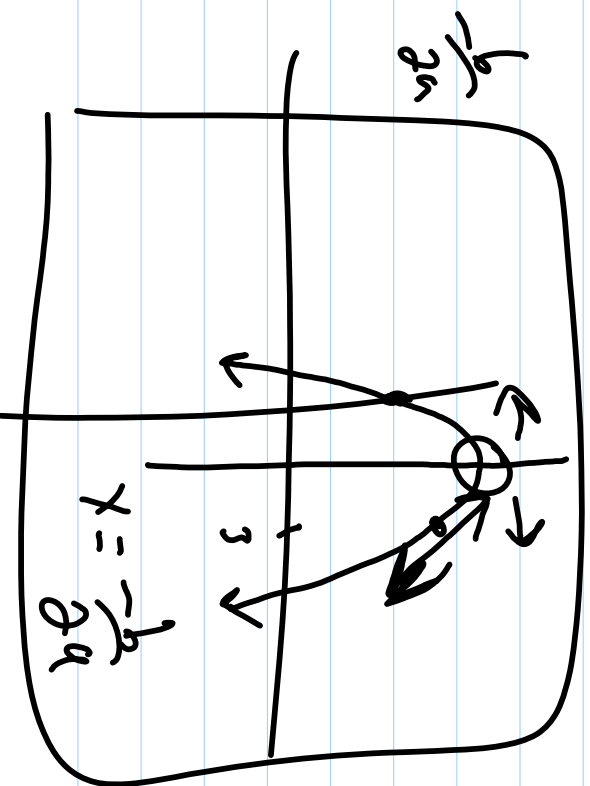
$$X = \frac{\log \frac{1}{36}}{\log \frac{1}{6}}$$

$$b) h(t) = -4.9t^2 + 19t + 1$$

a) ABOC [0,1] re.

$$A_{BOC} = \frac{h(1) - h(0)}{1 - 0} = \frac{10.1 - 1}{1} = \boxed{9.1} \text{ m/s}$$

b) your method!!



$$x = -\frac{(14)}{2(-4.5)}$$

$$7) \frac{2 \sin x}{1 - \cos x} = 1 - \sin x + \cos x (\tan x + 1) = 1.4$$



$$\frac{1 - \cos^2 x}{1 - \cos x} = 1 - \sin x + \cos x \left(\frac{\sin x + \cos x}{\cos x} \right)$$

$$\frac{(1 + \cos x) \cancel{(1 - \cos x)}}{\cancel{(1 - \cos x)}} = 1 - \cancel{\sin x} + \cancel{\sin x} + \cos x$$

$$\begin{aligned} 8) & \log \left(\frac{(2x-y) - \cancel{2} \log(3x+2y)}{\cancel{2}} \right) - \log(x+y) \\ &= \log \left[\frac{2x-y}{(3x+2y)^2} \right] - \log(x+y) \\ &= \log \frac{2x-y}{(3x+2y)^2} \left(\frac{1}{x+y} \right) \\ &= \log \frac{(2x-y)}{(3x+2y)^2 (x+y)} \end{aligned}$$

Q.)

$$r = \frac{2N}{K} \quad \text{or} \quad K = \frac{2N}{r} = \frac{2N}{\frac{2N}{r}} = r$$

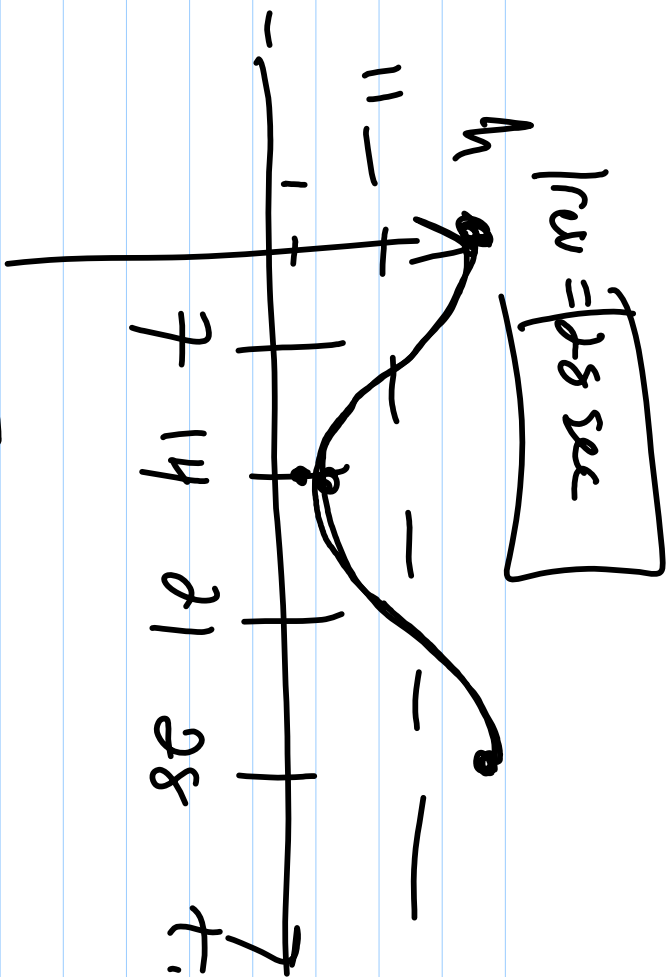
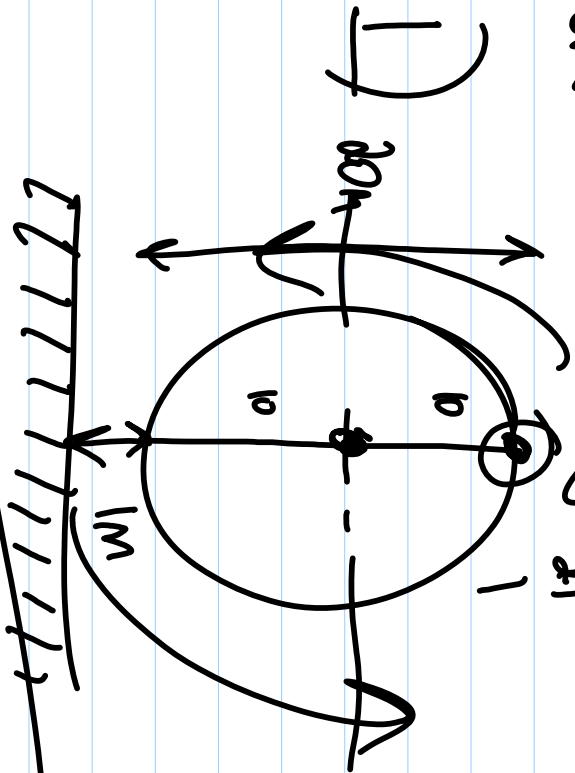
Ans $\frac{2}{\pi}$

$\frac{2}{\pi} \rightarrow$

$$y = n(\text{or } K(X-d)) + C.$$
$$= 2 \cos 2 \left(X - \frac{\pi}{2} \right) + 2.$$

vs \rightarrow

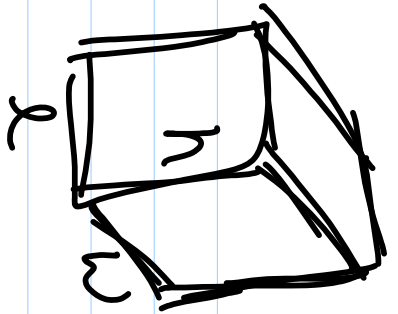
Part C: Thinking



$$h(t) = 10 \cos\left[\frac{\pi}{14}\right](t) + 11$$

$$k = \frac{2\pi}{28} = \frac{2\pi}{14} = \frac{\pi}{7}$$

2)



$$(18+x) \\ (20+x) \\ (6+x)$$

$$V \geq 5280$$

$$(18+x)(20+x)(6+x) \geq 5280$$

$$V = (18+x)(20+x)(6+x)$$

≥ 0

Q2-T

$$\sim) f(x) = \frac{ax+b}{cx+d}$$

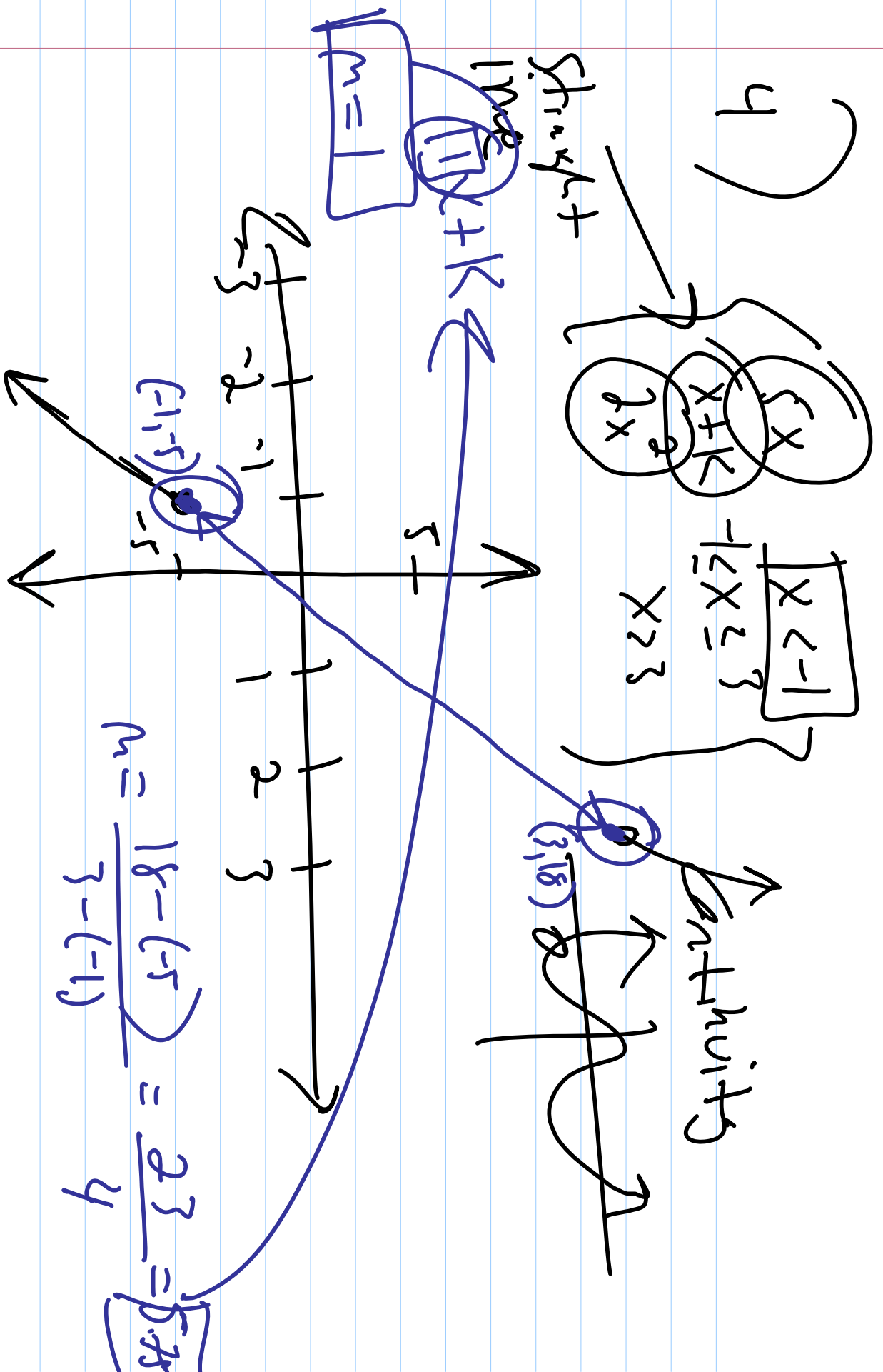
$$= \frac{ax+b}{(3x+2)}$$

$$= \frac{4x+b}{3x+2}$$

$$= \frac{4x-1}{3x+2}$$

VA:

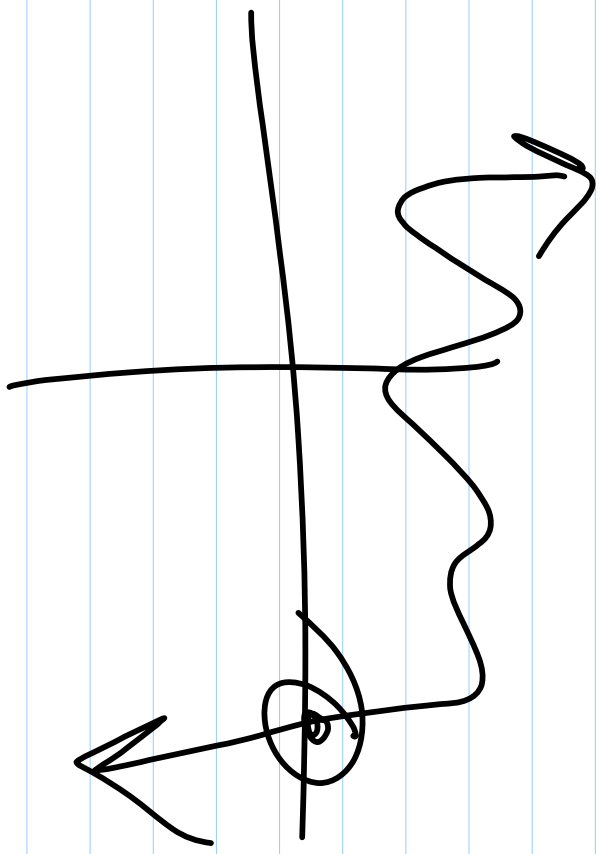
$$\boxed{x = -\frac{d}{c}}$$
$$3x = -2$$
$$(3x+2) = 0$$



Part D
1) $y_{t+1} = 4 - 3x_t$
 $y_t = 4$

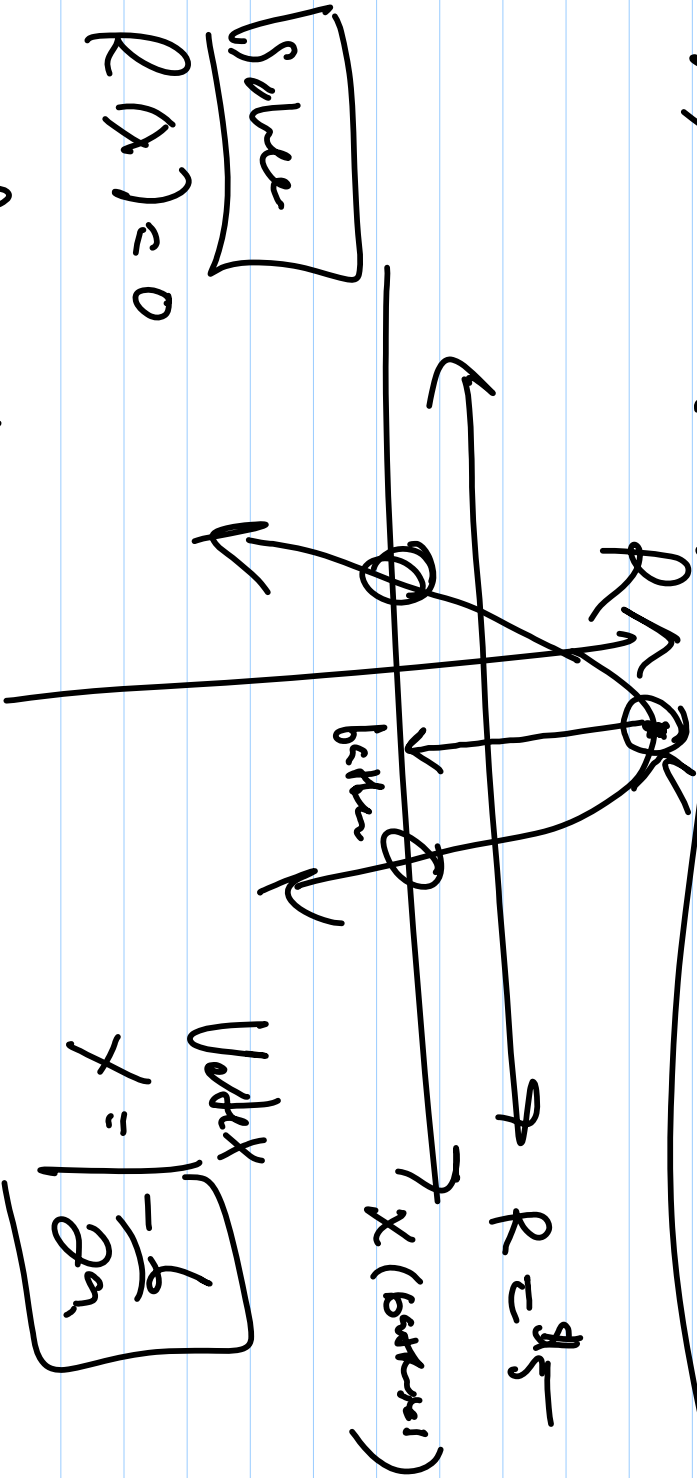
$y_{t+1} = 4 - 6x_t$
 $x_{t+1} = 4 - 6x_t$
Stable
Silver

2) $t = 7$



3)

$$R(x) = -x^2 + 16x + 30000$$

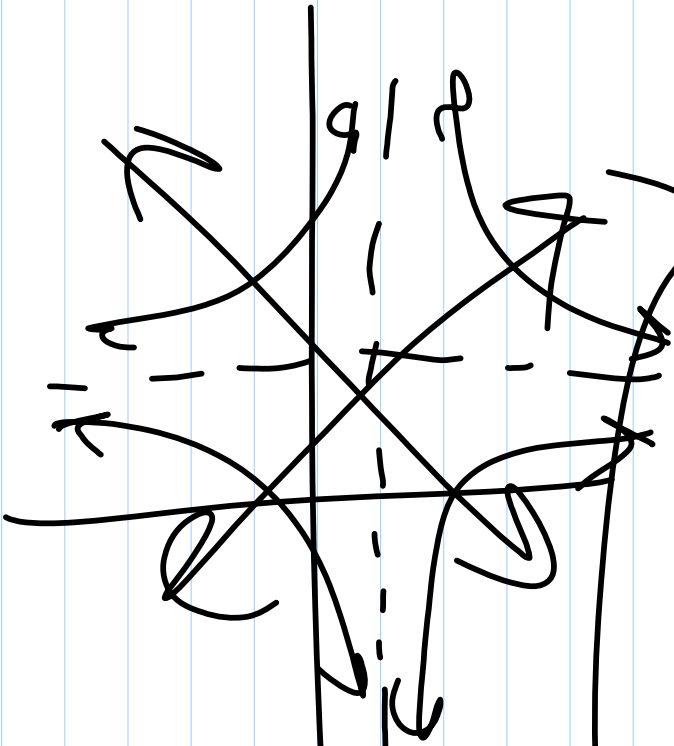


$$R(x) > 5$$

$$\text{MAX } y = \frac{D}{C} \quad x = -\frac{b}{2a}$$

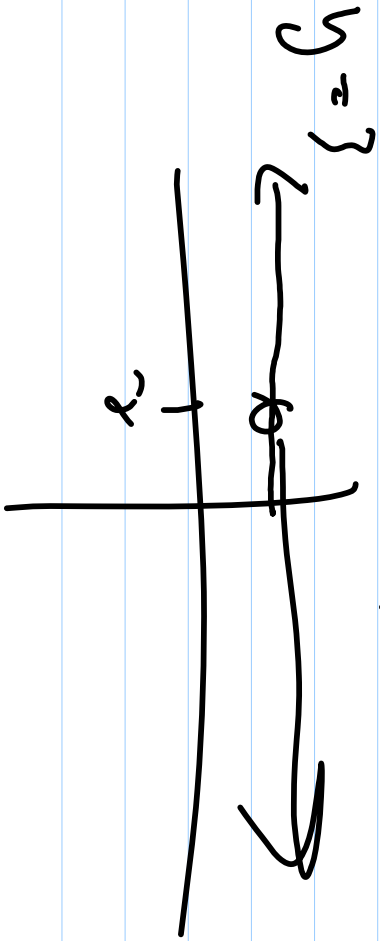
21)

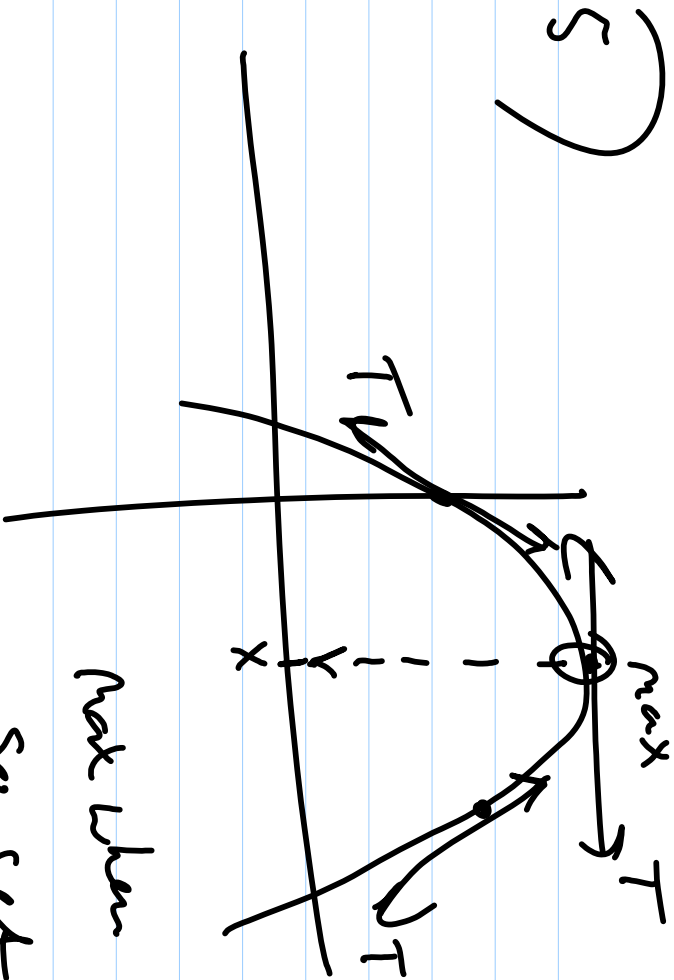
$$f(x) = \frac{ax+b}{cx+d} = \frac{3x+6}{2x+9}$$



$$= \frac{3x+6}{2x+9}$$

$$= \frac{3(x+2)}{2(x+4.5)}$$





max when $M_T = 0$

so set $f'(x) = 0$ and

solve for x .